Exposé court

46 Log-behaviour of quasi-polynomial-like functions

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By a quasi-polynomial-like function, we mean any function f(n) which grows as fast as a polynomial and takes the form

$$f(n) = t_k(n)n^k + t_{k-1}(n)n^{k-1} + \dots + t_d(n)n^d + o(n^d),$$

where the coefficients $t_d(n), \ldots, t_k(n) \in \mathbb{R}$ might depend on the residue class of n modulo some positive integer $M \ge 2$. For those types of functions, we investigate both the r-log-concavity problem and the higher order Turán inequalities. In particular, we apply the obtained results and deduce the analogous criteria in the case of the restricted partition function $p_{\mathcal{A}}(n,k)$ — that is the number of partitions of n with parts in a given mulitset $\{a_1, a_2, \ldots, a_k\}$ of positive integers.