## Exposé court

## 148 Divisibility by 2 on quartic models of elliptic curves and rational Diophantine $D(q)$-quintuples

## Yesin, Tuğba (Sabancı University)

Let $C$ be a smooth genus one curve described by a quartic polynomial equation over the rational field $\mathbb{Q}$ with $P \in C(\mathbb{Q})$. In this talk, I'll describe joint work with Mohammad Sadek, giving an explicit criterion for the divisibility-by-2 of a rational point on the elliptic curve ( $C, P$ ). This generalizes the classical criterion of the divisibility-by-2 on elliptic curves described by Weierstrass equations.

We also employ this criterion to investigate the question of extending a rational $D(q)$-quadruple to a quintuple. We give concrete examples to which we can give an affirmative answer. One of these results implies that although the rational $D(16 t+9)$-quadruple $\{t, 16 t+8,225 t+14,36 t+20\}$ can not be extended to a polynomial $D(16 t+9)$-quintuple using a linear polynomial, there are infinitely many rational values of $t$ for which the aforementioned rational $D(16 t+9)$-quadruple can be extended to a rational $D(16 t+9)$-quintuple. Moreover, these infinitely many values of $t$ are parametrized by the rational points on a certain elliptic curve of positive Mordell-Weil rank.

