Exposé court

13 Avoiding problems Ballini, Francesco (University of Oxford)

In 2020 Masser and Zannier proved that "most" abelian varieties over the algebraic numbers are not isogenous to any jacobian; here "most" refers to an ordering by some height function. We discuss some analogous problems in powers of the modular curve Y(1), for instance: given a curve $C \subseteq Y(1)^2$, how can we find a rational point $(p, q) \in Y(1)^2$ which is not isogenous to any point $(x, y) \in C$ (meaning that p and x - resp. q and y - represent isogenous elliptic curves)?